

Fast minimum-norm adversarial attacks through adaptive norm constraints

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Adversarial Robustness Evaluation

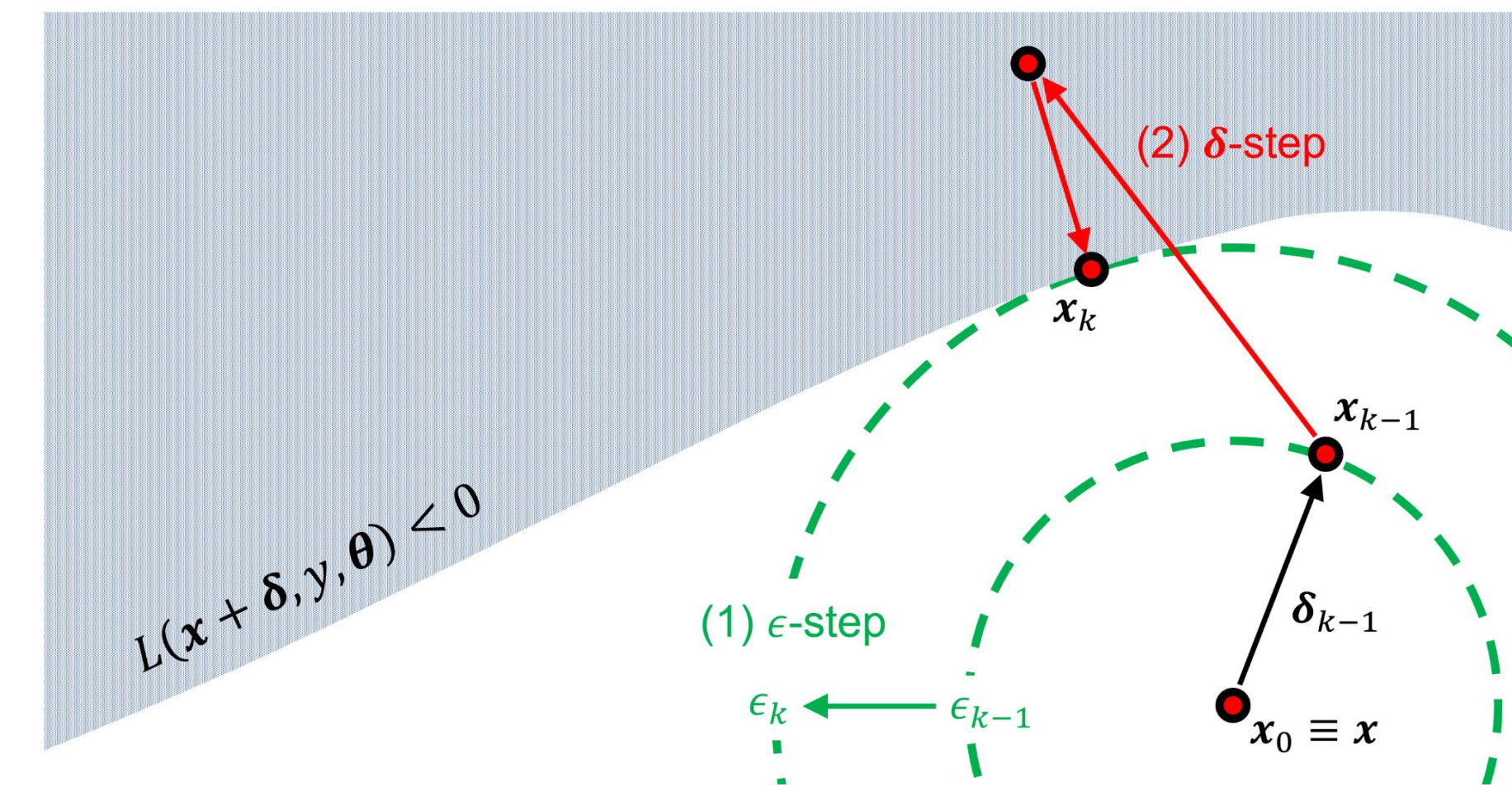
Evaluating adversarial robustness amounts to finding the minimum norm perturbation to have input samples misclassified

$$\delta^* \in \arg \min_{\delta} \|\delta\|_p, \quad \text{s.t. } L(x + \delta, y, \theta) < 0, \quad x + \delta \in [0, 1]^d$$

Limitations of state-of-the-art attacks

- they require many iterations to converge to good local optima;
- they require careful and computationally-demanding hyperparameter tuning; and
- they are specific to a given perturbation model.

Fast Minimum-norm Adversarial Attack

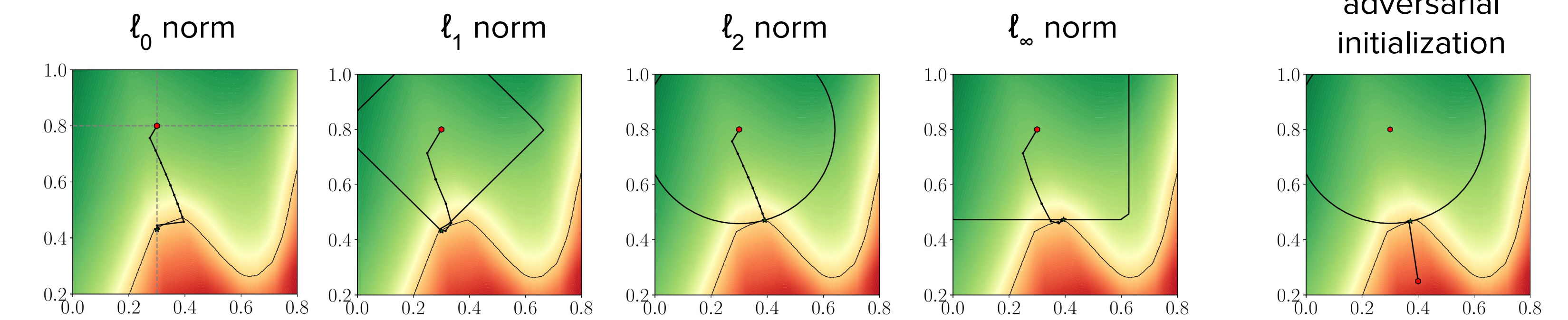


epsilon-step (1): decision-based adaptation of the search region (increase radius if x_i is not adversarial, reduce if x_i is adversarial)

delta-step (2): follows gradient direction and projects in the search region

Key aspects

Works in different ℓ_p norms



Attack Algorithm

Algorithm 1 Fast Minimum-norm (FMN) Attack

Input: x , the input sample; t , a variable denoting whether the attack is targeted ($t = +1$) or untargeted ($t = -1$); y , the target (true) class label if the attack is targeted (untargeted); γ_0 and γ_K , the initial and final ϵ -step sizes; α_0 and α_K , the initial and final δ -step sizes; K , the total number of iterations.

Output: The minimum-norm adversarial example x^* .

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1:  $x_0 \leftarrow x, \epsilon_0 = 0, \delta_0 \leftarrow 0, \delta^* \leftarrow \infty$ 
2: for  $k = 1, \dots, K$  do
3:    $g \leftarrow t \cdot \nabla_{\delta} L(x_{k-1} + \delta, y, \theta)$  // loss gradient
4:    $\gamma_k \leftarrow h(\gamma_0, \gamma_K, k, K)$  //  $\epsilon$ -step size decay (Eq. 7)
5:   if  $L(x_{k-1}, y, \theta) \geq 0$  then
6:      $\epsilon_k = \|\delta_{k-1}\|_p + L(x_{k-1}, y, \theta) / \|g\|_q$  // adversarial not found yet else  $\epsilon_k = \epsilon_{k-1} (1 + \gamma_k)$ 
7:   else
8:     if  $\|\delta_{k-1}\|_p \leq \|\delta^*\|_p$  then
9:        $\delta^* \leftarrow \delta_{k-1}$  // update best min-norm solution
10:    end if
11:     $\epsilon_k = \min(\epsilon_{k-1} (1 - \gamma_k), \|\delta^*\|_p)$ 
12:  end if
13:   $\alpha_k \leftarrow h(\alpha_0, \alpha_K, k, K)$  //  $\delta$ -step size decay (Eq. 7)
14:   $\delta_k \leftarrow \delta_{k-1} + \alpha_k \cdot g / \|g\|_2$ 
15:   $\delta_k \leftarrow \Pi_{[0, 1]^d}(x_0 + \delta_k) - x_0$ 
16:   $\delta_k \leftarrow \text{clip}(x_0 + \delta_k) - x_0$ 
17:   $x_k \leftarrow x_0 + \delta_k$ 
18: end for
19: return  $x^* \leftarrow x_0 + \delta^*$ 

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Experimental setup

- tested on 9 models (MNIST, CIFAR10, ImageNet)
- compared against 4 state-of-the-art minimum-norm attacks
- evaluated in targeted and untargeted scenario

Evaluation metrics

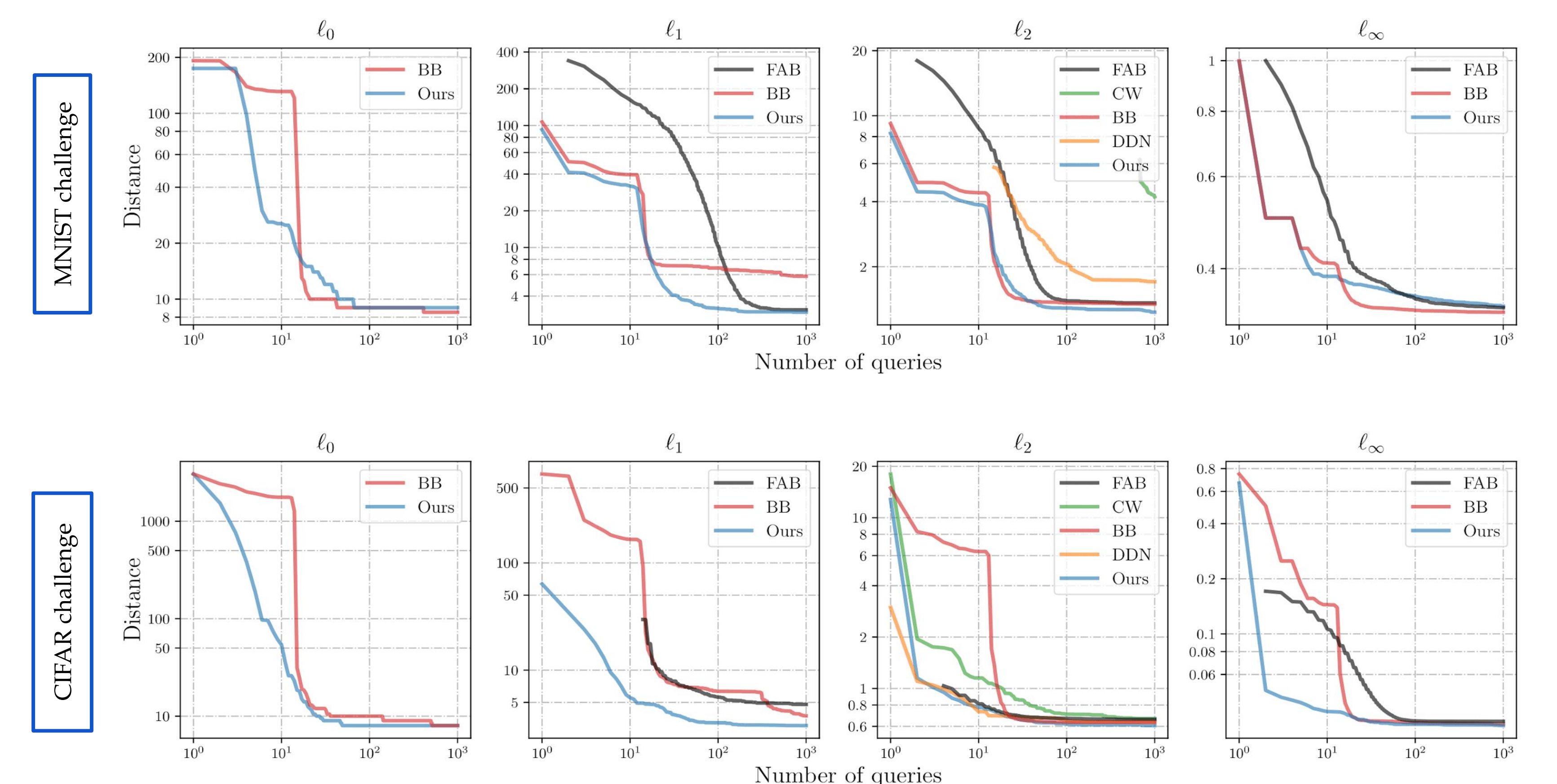
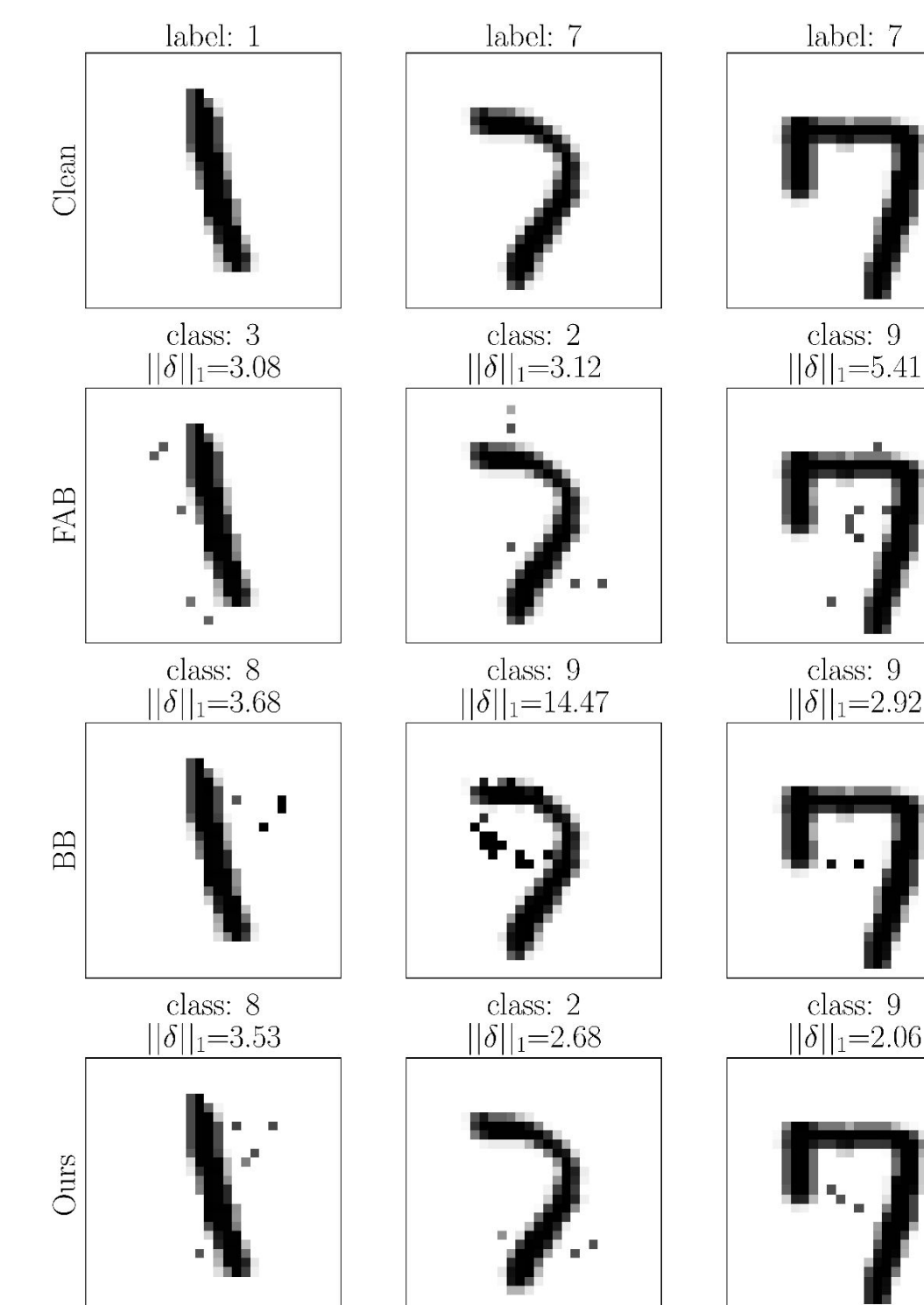
- median distance found after 1000 queries
- avg. time per query
- convergence speed
- robustness to hyperparameter choice

Median norm of perturbation $\|\delta^*\|_p$ found for 1000 queries

Model	MNIST				CIFAR10									
	M1	M2 [6]	M3[4]	M4[7]	M1	M2 [6]	M3[4]	M4[7]	C1[6]	C2[5]	C3[4]	C1[6]	C2[5]	C3[4]
ℓ_0 [1] BB	12	152	52	145	20	179	39	183	28	44	32	29	65	33
Ours	9	21	18	15	16	41	28	55	11	17	16	25	38	32
ℓ_1 [3] FAB	8.662	225.728	163.879	312.314	-	-	-	-	7.017	10.199	17.134	11.412	15.265	23.367
[1] BB	10.604	49.834	17.570	46.994	16.602	53.114	29.885	54.312	4.280	4.821	9.516	8.506	10.405	17.316
Ours	7.125	3.535	13.656	4.989	13.176	6.590	21.371	12.156	4.280	4.821	9.516	8.506	10.405	17.316
ℓ_2 [3] FAB	1.540	1.591	2.808	16.303	-	-	-	-	0.773	1.113	1.061	-	-	-
[2] CW	1.633	5.151	3.706	-	2.502	-	4.719	-	0.865	0.997	0.987	1.360	2.900	1.554
[1] BB	1.747	1.818	3.016	4.571	2.638	2.589	3.519	5.313	0.856	0.950	1.097	1.252	1.455	1.732
[4] DDN	1.471	2.013	2.616	1.147	2.308	2.717	3.363	1.960	0.658	0.771	0.910	1.113	1.307	1.398
Ours	1.615	1.089	2.607	1.563	2.302	1.555	3.244	2.407	0.672	0.741	0.910	1.091	1.281	1.380
ℓ_{∞} [3] FAB	0.148	0.365	0.248	0.900	-	-	-	-	0.038	0.052	0.029	-	-	-
[1] BB	0.159	0.336	0.243	0.409	0.223	0.361	0.280	0.477	0.044	0.054	0.029	0.059	0.074	0.042
Ours	0.140	0.278	0.233	0.408	0.206	0.326	0.277	0.434	0.034	0.042	0.024	0.057	0.066	0.037

Experiments

ℓ_1 norm adversarial examples on MNIST challenge model

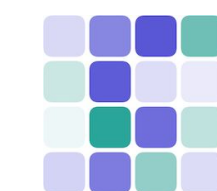


Useful links and implementations

Preprint: <https://arxiv.org/abs/2102.12827>

Available implementations:

- <https://github.com/pralab/Fast-Minimum-Norm-FMN-Attack>
- <https://github.com/bethgelab/foolbox>
- <https://github.com/jeromeronv/adversarial-library>
- <https://github.com/pralab/secml>



Key results

FMN combines desirable traits of minimum-norm attacks to help improve current adversarial evaluations by:

- finding smaller or comparable minimum-norm perturbations in different ℓ_p norms;
- being less sensitive to hyperparameter choices; and
- being extremely fast by converging quickly and by performing lightweight steps.

We provide extensive experiments and the open source implementation of the attack.

Future work

Extension towards minimum-norm adaptive evaluations. Improvements that have been suggested for PGD, such as momentum, cyclical step sizes and restarts. Improvements that overcome obfuscated gradients (e.g. gradient smoothing)

References

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- [3] F. Croce and M. Hein. Minimally distorted adversarial examples with a fast adaptive boundary attack. ICML 2020.
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- [7] H. Zhang *et al.* Towards stable and efficient training of verifiably robust neural networks. ICLR 2020.

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